

$$Q_m = m(m+2) \sum_{n=1}^{\infty} \left( \frac{r^{2n}}{n^2} \right) = \frac{r^2}{6} (m+1)$$